

# Power Distribution System Losses

Tao Hong, PhD

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[hongtao01@gmail.com](mailto:hongtao01@gmail.com)

<http://www.linkedin.com/in/hongtao>

[www.DrHongTao.com](http://www.DrHongTao.com)

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# Tao Hong

- Experience

- *Analytical Consultant, SAS Institute Inc.*
  - Revenue optimization, retail forecasting, demand response
- *Business Knowledge Series Instructor, SAS Institute Inc.*
  - SAS for Electric Load Forecasting
- *Engineer, Sr. Engineer, Principal Engineer, Quanta Technology, LLC.*
  - Load forecasting, T&D planning, system loss evaluation, system reliability analysis, load modeling, renewable energy

- Education

- Ph.D.      E.E., O.R.,      NC State University, Raleigh
- M.S.      E.E., I.E., O.R.,      NC State University, Raleigh
- B.Eng,      Automation,      Tsinghua University, Beijing

# Outline

- Overview
- Fundamentals
- Transformer Losses
- Line Losses
- Capacitor Application

This presentation can be downloaded from the course webpage:

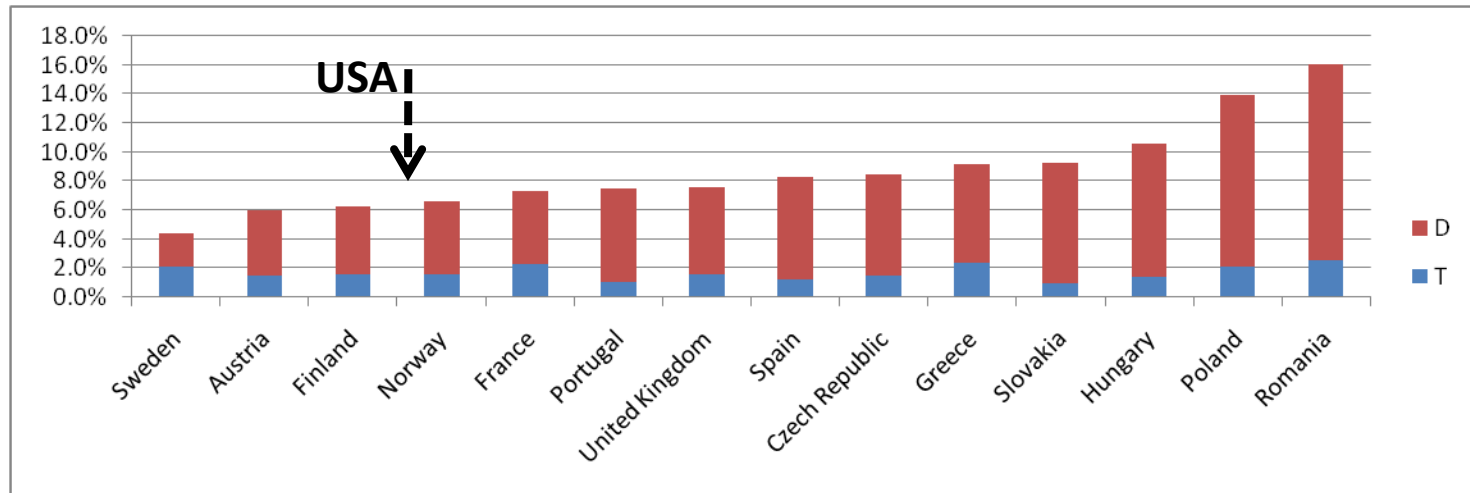
<http://courses.DrHongTao.com/pds1>

# Why Do We Study Losses?

- Cost of energy and capital
- Difficulties in siting new generation
- Pressure from regulators
- Better understanding of customer behaviors
- More defensible load forecasting
- System planning

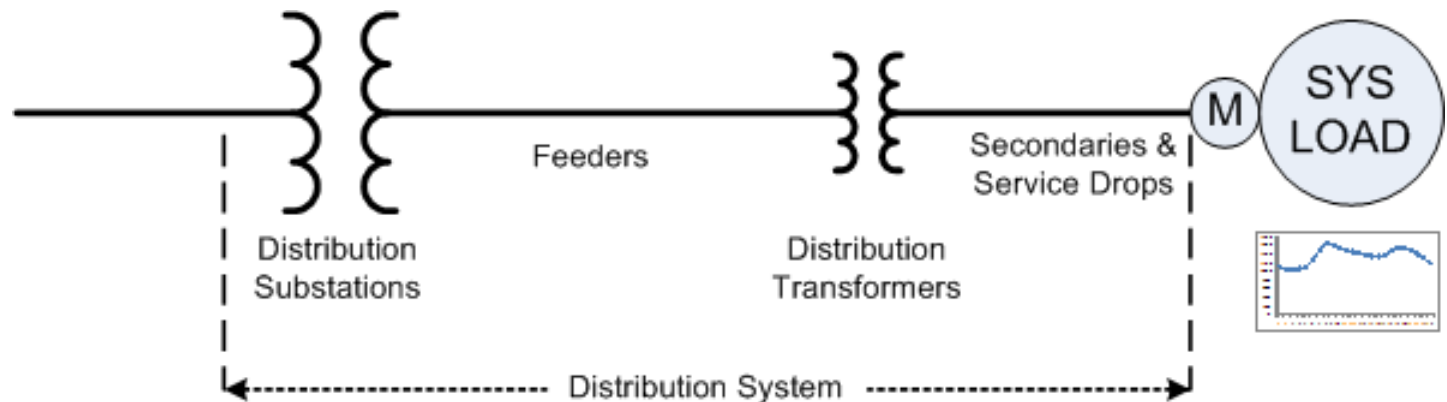
# T&D Losses

- A tentative definition
  - “Energy Produced minus Energy Sold”
- T&D losses in USA
  - 6.6% (1997), 6.5% (2007)
- T&D losses in Europe

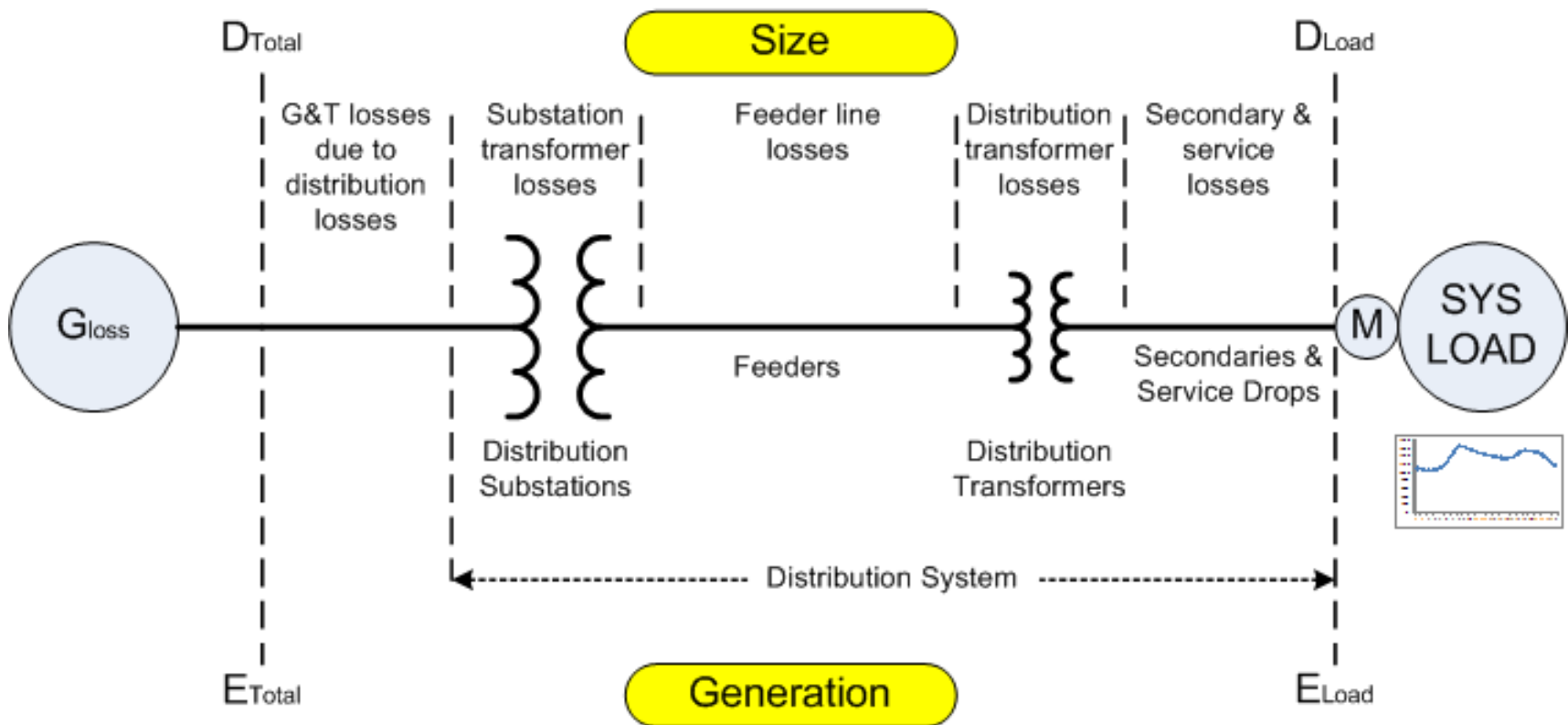


# A Simplified Distribution System

- Distribution system
  - Daily load
  - System peak



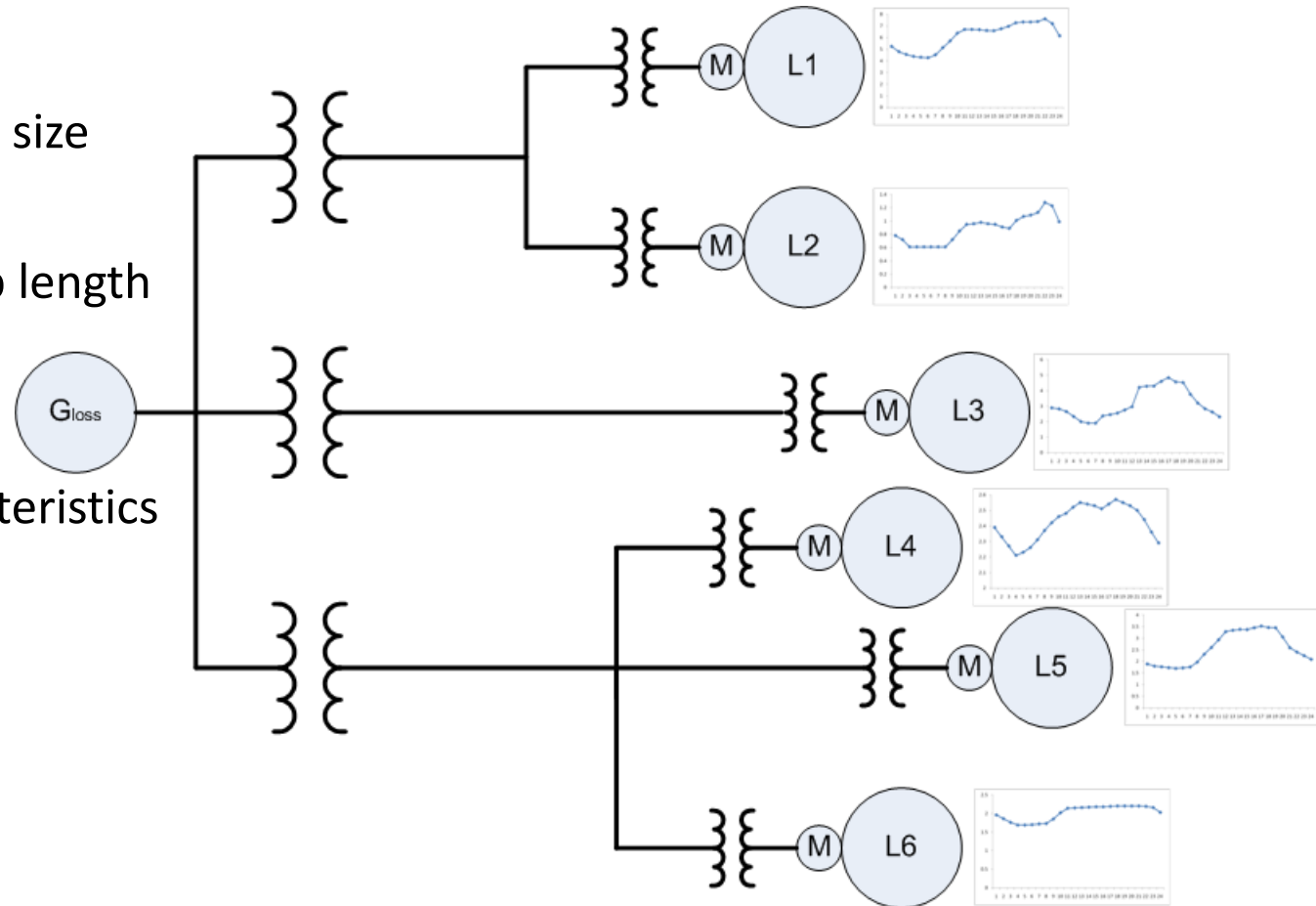
# Loss Generator



# A Realistic Distribution System

- Variables

- Transformer size
- Line length
- Service drop length
- Load curves
- Load levels
- Load characteristics

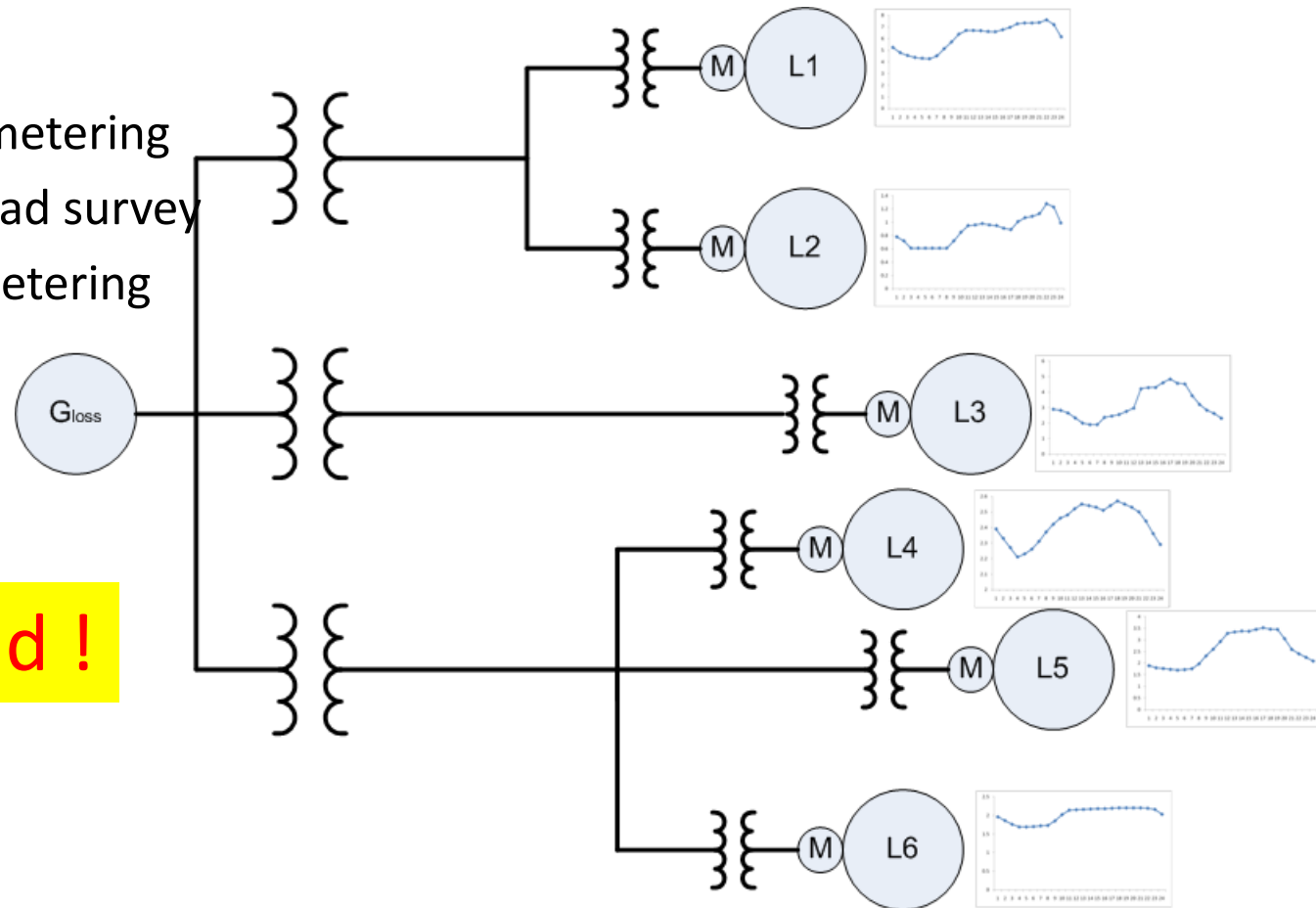




# Metering and Data

- Sources

- Substation metering
- Customer load survey
- Customer metering
- TLM
- ...

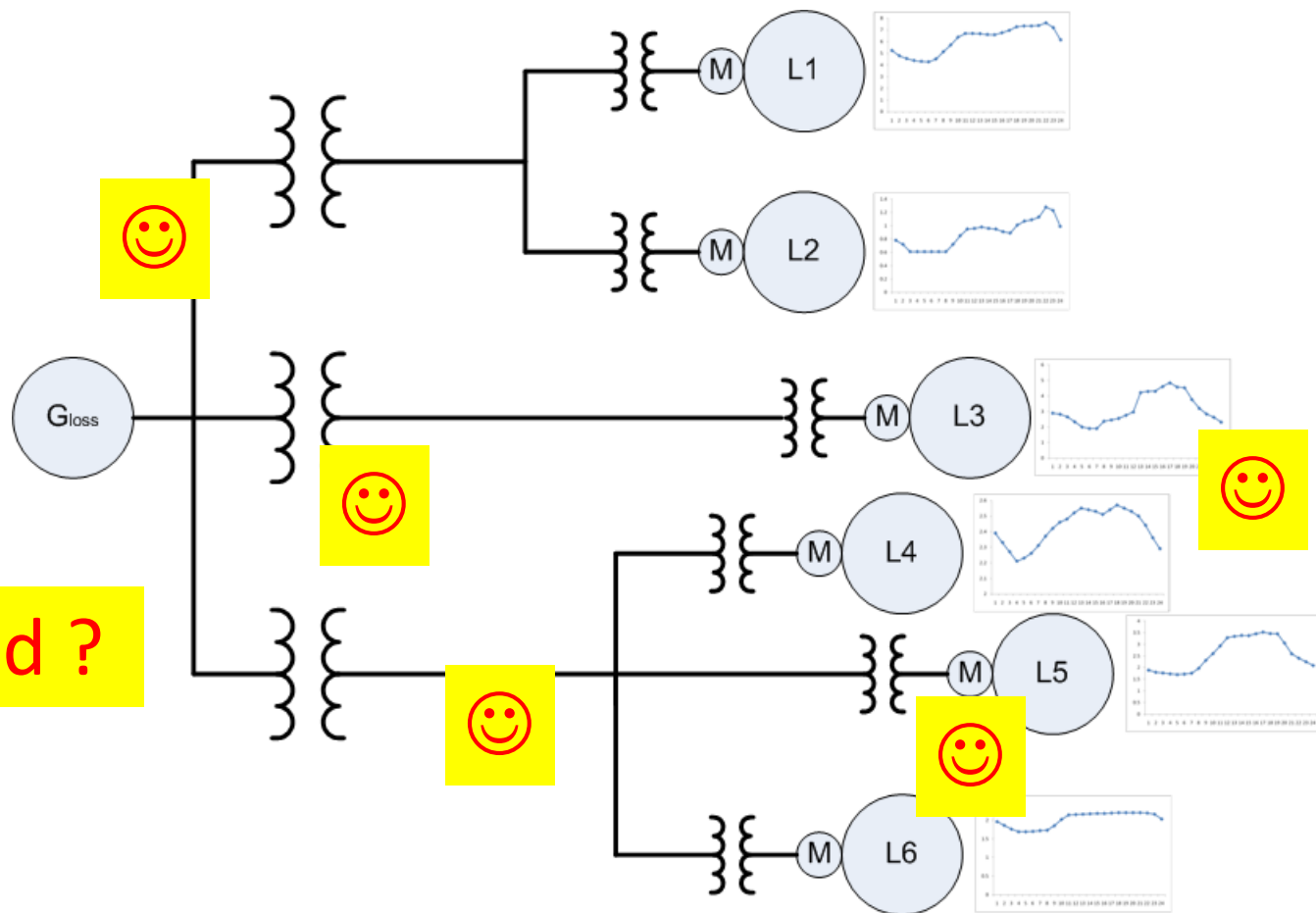


Smart Grid !

# Loss Management

- Analyze...
- Optimize...

Smart Grid ?



# Definitions

- System losses
  - Demand losses
  - Energy losses
- Equipment losses
- No load losses
- Load Losses

# Calculation

- Substation transformers
- Feeders
- Distribution transformers
- Secondary losses
- Capacitors
- Unmetered load and theft

# Causes

- Poor power factor on the distribution feeder
- Conductor sizing and arrangement
- Load imbalance between feeders
- Imbalance between phase A, B, C
- Load/no-load losses in distribution transformers
- Improper Volt/VAR control (regulator/LTC settings, line cap controls, blown fuses on cap banks, etc.)
- Extremely long distribution lines

# Mitigation

- Increase conductor size
- Proper distribution transformer size and design (no load and load)
- Balance currents in phases
- Share loads equally between circuits
- Optimize feeder configuration at each voltage level
- Add feeder capacitors
- Reduce harmonics
- High efficiency loads

## Mitigation (*Continued*)

- Higher primary voltages
- Lower secondary voltages (usually)
- Proper distribution substation design and operation
- Capacitor bank inspection of fuses
- Primary selective systems as opposed to secondary network systems
- Eliminate transformations, where possible
- Replace low efficiency and overloaded transformers
- Proper capacitor control

## Mitigation (*Continued*)

- Load control (demand side management)
- Amorphous steel transformers
- Reduce load factor by reducing peak loads
- Retire low efficiency cable
- Open tie at substations, with multiple transformers, to reduce circulating currents or match transformer impedances

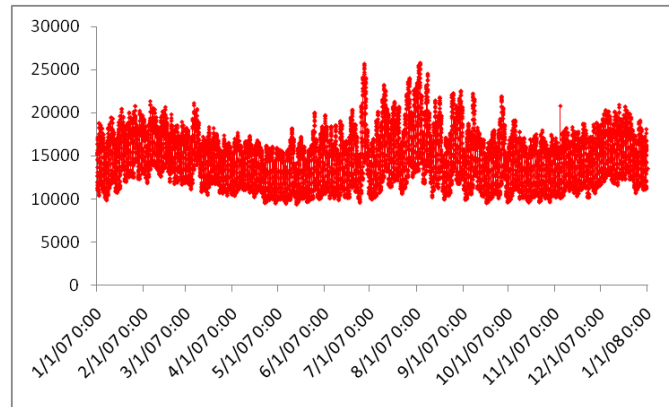


Overview	Introduction
Fundamentals	Basic concepts
Transformer Losses	Definitions
Line Losses	Calculation
Capacitor Application	Causes and mitigation

# Q/A

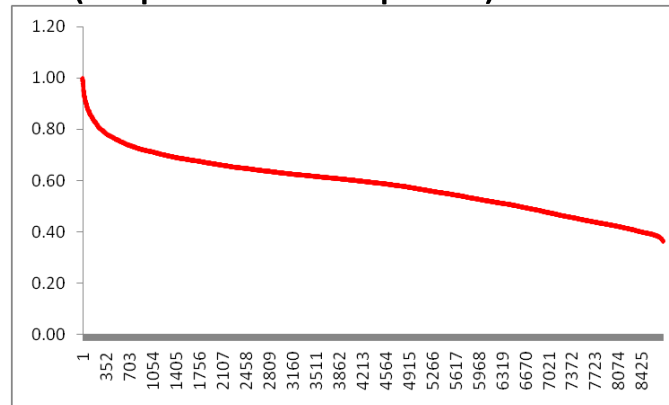
# Load Duration Curve

- Load curve



- Load duration curve

- Descending order of load (in per unit of peak)



Power Distribution System Losses

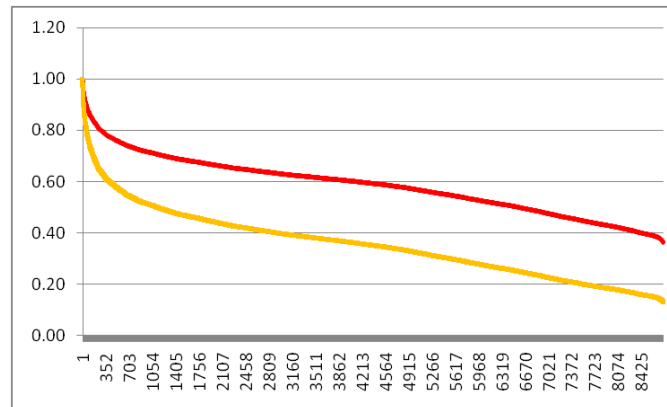
# Load Factor

- Average load, in per unit of peak, over a predetermined period of time

$$\text{Load Factor} = \frac{\text{kWh of Load During a Specified Time Period}}{(\text{Hours in Time Period})(\text{Peak kW Load})}$$

# Loss Duration Curve

- Load losses are proportional to the square of the loading
  - ~~Average losses are proportional to the square of average load~~
  - ~~Average losses are proportional to the square of load factor~~
- Loss duration curve
  - Square of load duration curve



# Loss Factor

- Average loss, in per unit of peak, over a predetermined period of time

$$\text{Loss Factor} = \frac{\text{kWh of Loss During a Specified Time Period}}{(\text{Hours in Time Period})(\text{Peak kW Loss})}$$

# Loss Factor

- Empirical formula

$$\text{Loss Factor} = C(\text{Load Factor}) + (1 - C)(\text{Load Factor})^2$$
$$C \in [0.15, 0.3]$$

# Coincidence Factor

- The ratio of the maximum demand of a set of users to the sum of the set's individual maximum demands

$$\text{Coincidence Factor} = \frac{\left\| \sum_{i=1}^N D_i \right\|_{\infty}}{\sum_{i=1}^N \|D_i\|_{\infty}}$$

# Coincidence Factor

- Empirical formula

$$\text{Coincidence Factor} = 0.5 \times \left(1 + \frac{5}{2N + 3}\right)$$



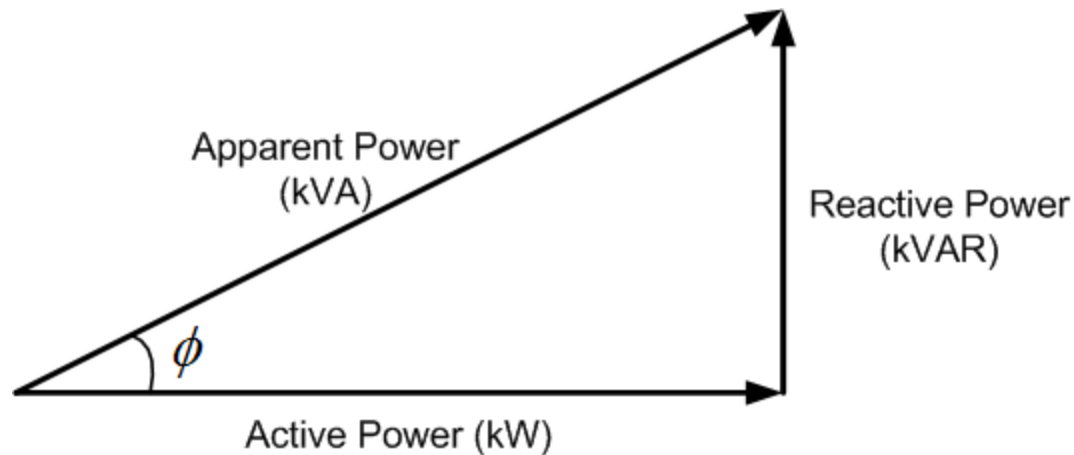
# Diversity Factor

- The inverse of coincidence factor

$$\text{Diversity Factor} = \frac{\sum_{i=1}^N \|D_i\|_{\infty}}{\left\| \sum_{i=1}^N D_i \right\|_{\infty}}$$

# Power Factor

- The ratio of active power to apparent power
  - $\cos\phi$
- 0.85 to 0.98



# Peak Responsibility Factor

- Peak load losses occur at peak load on a component
  - May not occur at system peak
  - Only a “fraction” of the individual peak losses contribute to system peak demand

$$\text{System Peak Responsibility Factor} = \frac{\text{Component kW Load at System Peak}}{\text{Component kW Peak Load}}$$

Question: “Fraction” = SPRF?

# Peak Responsibility Factor

- Fraction = SPRF?
  - SPRF is a ratio of loads
  - Losses are proportional to the square of loads
  - Losses are function of  $\text{SPRF}^2$
- Example
  - 1kW losses at its peak load
  - $\text{SPRF} = 0.8$
  - 0.64kW losses at system peak
  - Need additional 0.64kW generation and equipment to supply losses

# Peak Responsibility Factor

- Typical peak responsibility factor for transformers

Type	SPRF	SPRF <sup>2</sup>
Generator Step-up	1	1
Transmission substation	0.9	0.81
Distribution substation	0.8	0.64
Distribution	0.75	0.56

# Peak Responsibility Factor

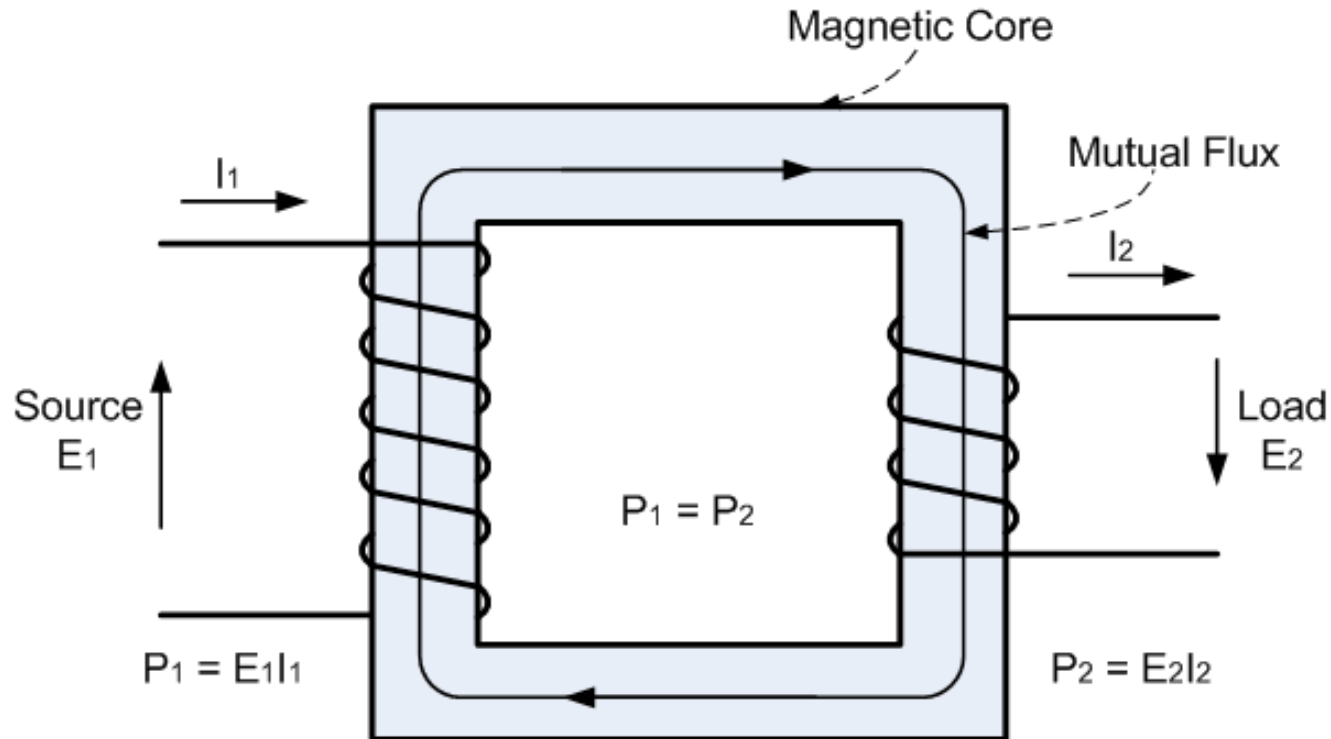
- Peak responsibility factors of one utility

	Distribution Sub	Feeder
Min	0.83	0
Q1	0.92	0.58
Average	0.93	0.71
Median	0.95	0.76
Q3	0.96	0.85
Max	0.98	1

# Q/A

# A Basic Transformer

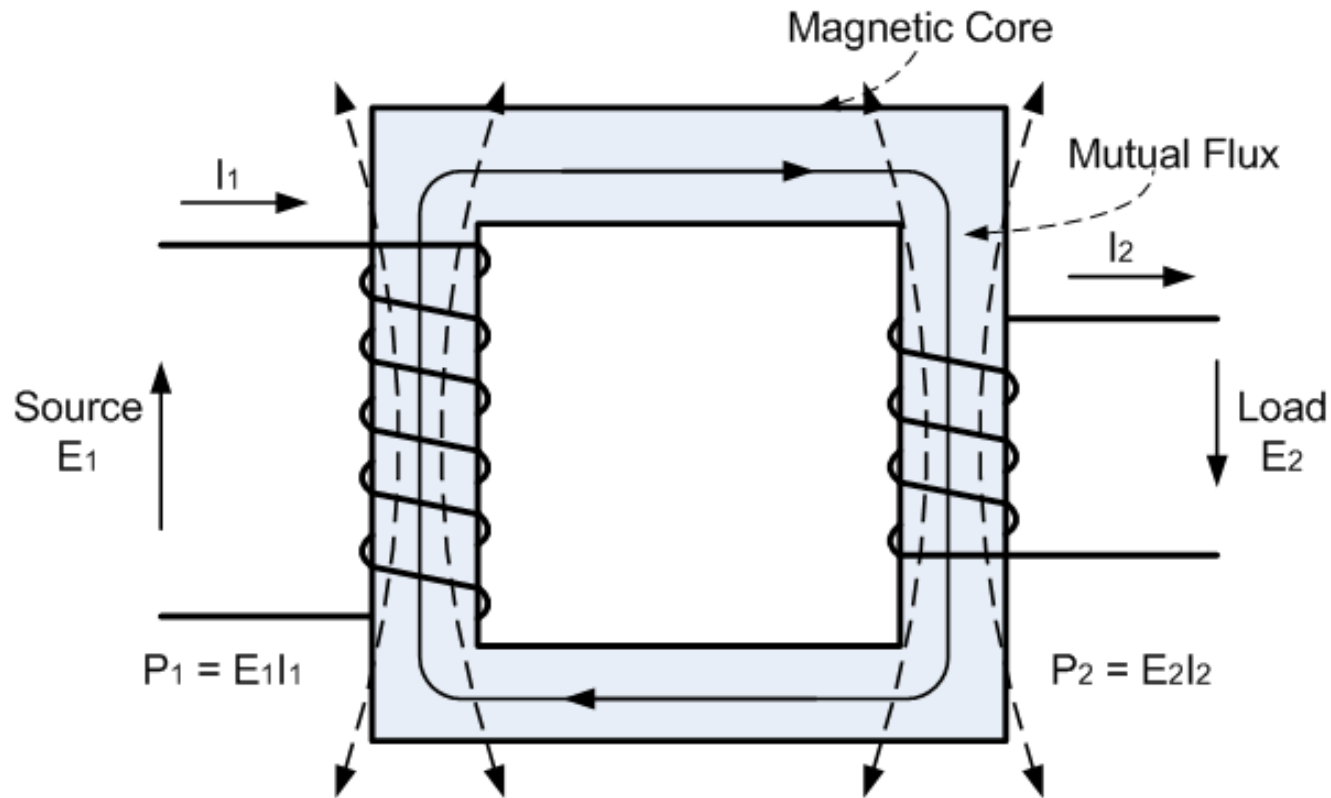
- Lossless transformer





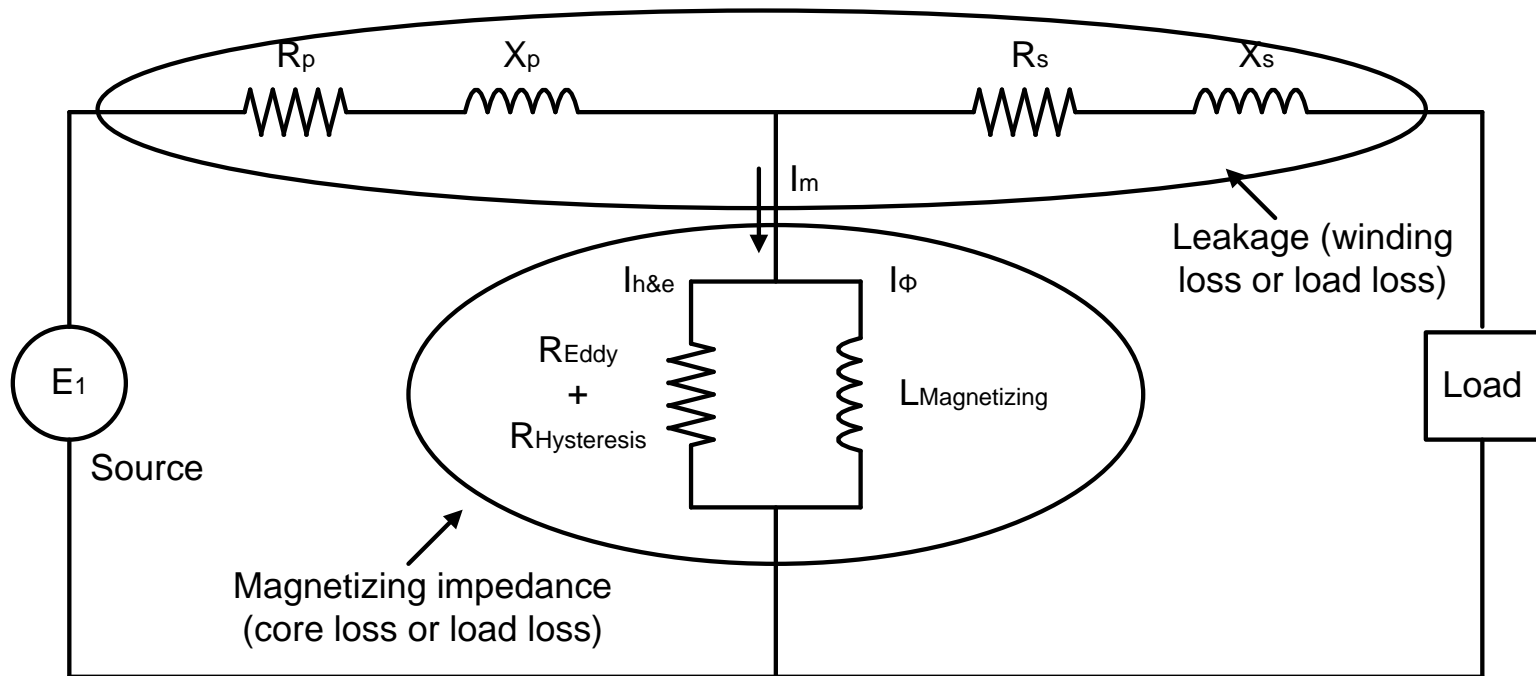
# A Basic Transformer

- Flux relations



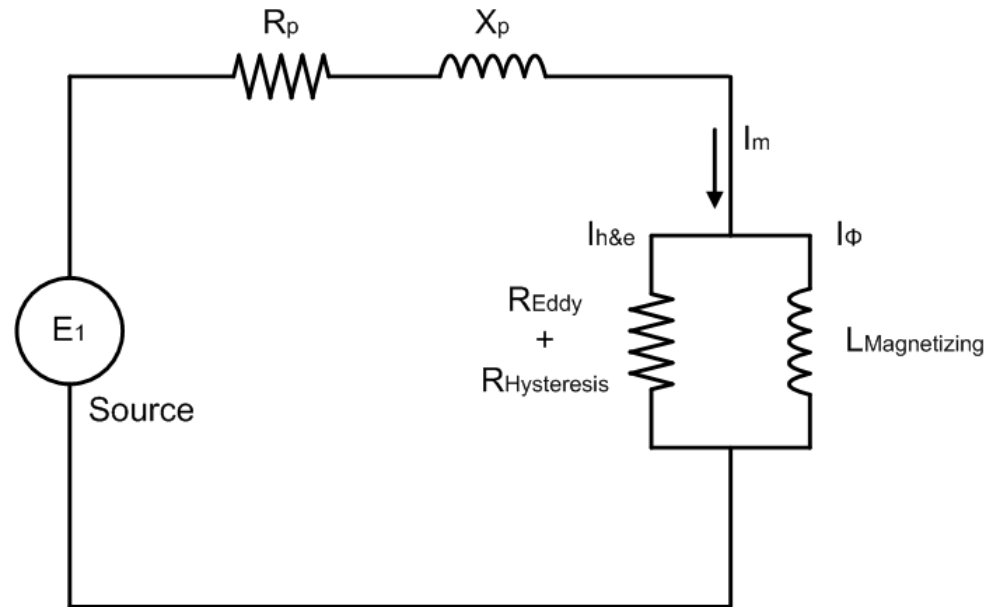
# Transformer Model

- Leakage impedance
- Magnetizing impedance



# No-load Losses

- Primary circuit



# No-load Losses

- No-load losses of a transformer
  - Eddy-current loss
  - Hysteresis loss
  - $I^2R$  loss caused by exciting current
  - Dielectric losses
- Due to the iron in the transformer core
  - Iron losses
  - FE losses

# No-load Losses

- Transformer no-load demand losses (TNLDL)
  - From data sheet
- Transformer no-load energy losses (TNLEL)

$$\text{Transformer No-Load Energy Losses} = \text{Transformer No-Load Demand Losses} \times 8760$$

# Load Losses

- Transformer load demand losses (TLDL)

$$\text{Transformer Load Demand Losses} = \text{Transformer Peak Load Demand Losses} \times \text{SPRF}^2$$

# Load Losses

- Transformer load energy losses (TLEL)

Transformer Load Energy Losses = Transformer Peak  
Load Demand Losses × Annual Loss Factor × 8760

# Reactive Losses

- Reactive demand losses
  - No-load reactive losses
  - Load reactive losses

Very Small

- Reactive energy losses

No Value?

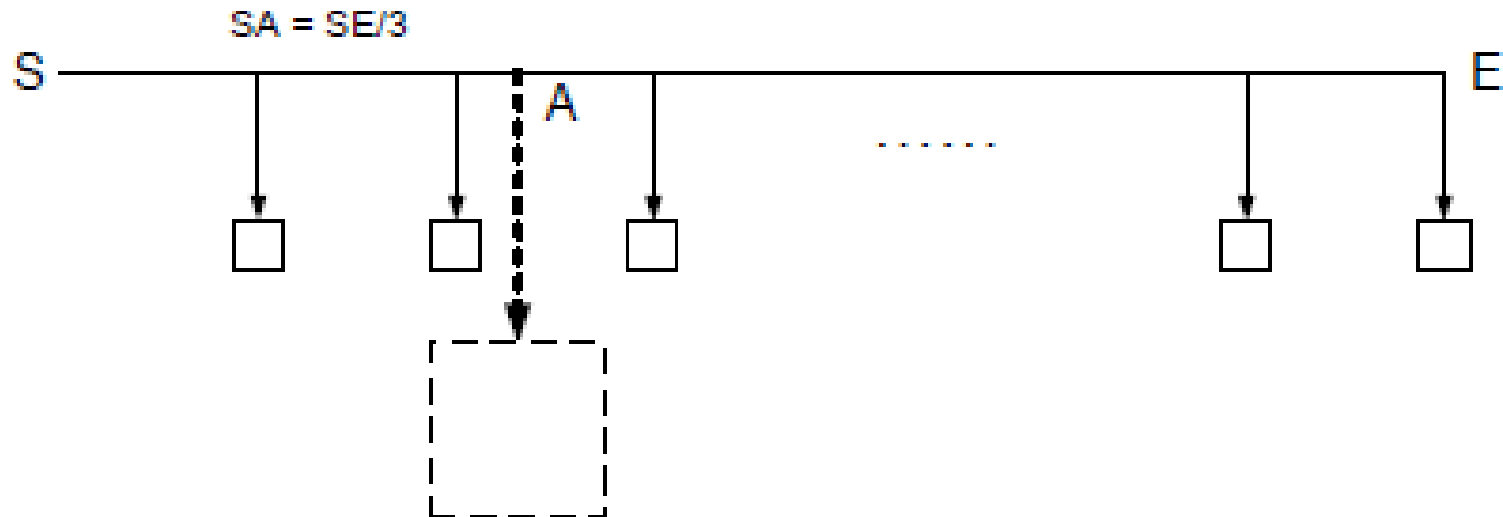


Overview	A basic transformer
Fundamentals	Transformer model
Transformer Losses	No-load losses
Line Losses	Load losses
Capacitor Application	Reactive losses

# Q/A

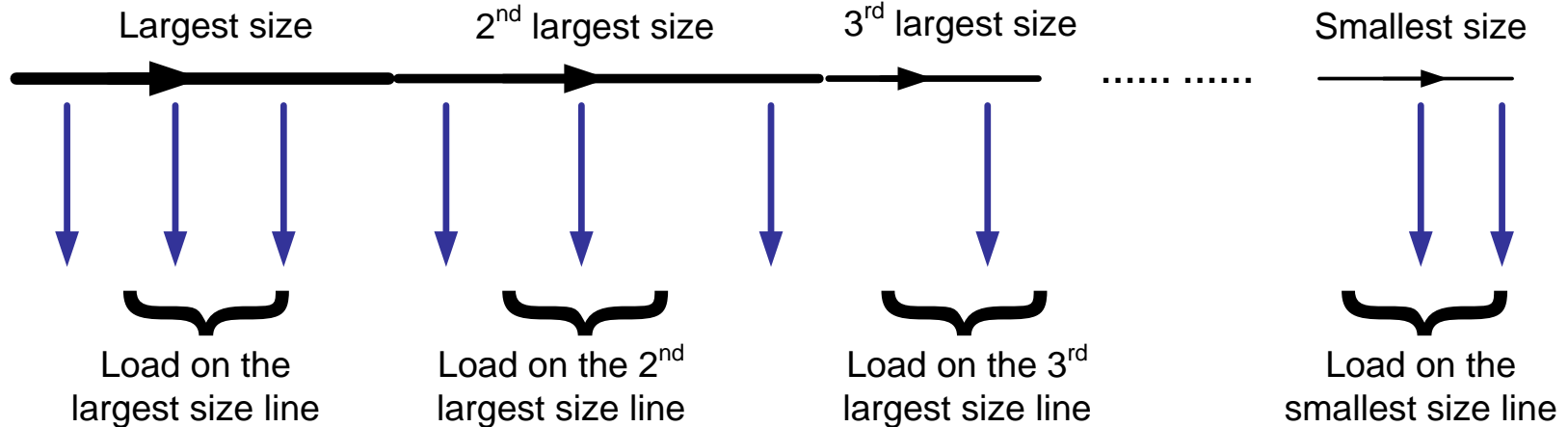
# 1/3 Rule

- For feeders with evenly distributed load and one conductor size
  - “1/3 Rule” for losses



# Generic Line Losses

- For a generic feeder



$$P_k = \frac{(I_{\max,k})^2 + I_{\min,k} I_{\max,k} + (I_{\min,k})^2}{3} R_k$$

# Primary Line Losses

- Peak load losses

Peak 3 $\phi$  Load Losses = 3 $\times$  Generic Line Losses

# Primary Line Losses

- Energy losses

$$\text{Primary Line Energy Losses} = \text{Peak } 3\phi \text{ Load Losses} \times \text{Loss Factor} \times 8760$$

# Primary Line Losses

- Demand losses

$$\text{Primary Line Demand Losses} = \text{Peak } 3\phi \text{ Load Losses} \times \text{SPRF}^2$$

# Lateral Line Losses

- Peak losses on a single phase lateral (including 100% neutral return)

$$\text{Peak } 3\phi \text{ Load Losses} = 2 \times \text{Generic Line Losses}$$

# Distribution Factor

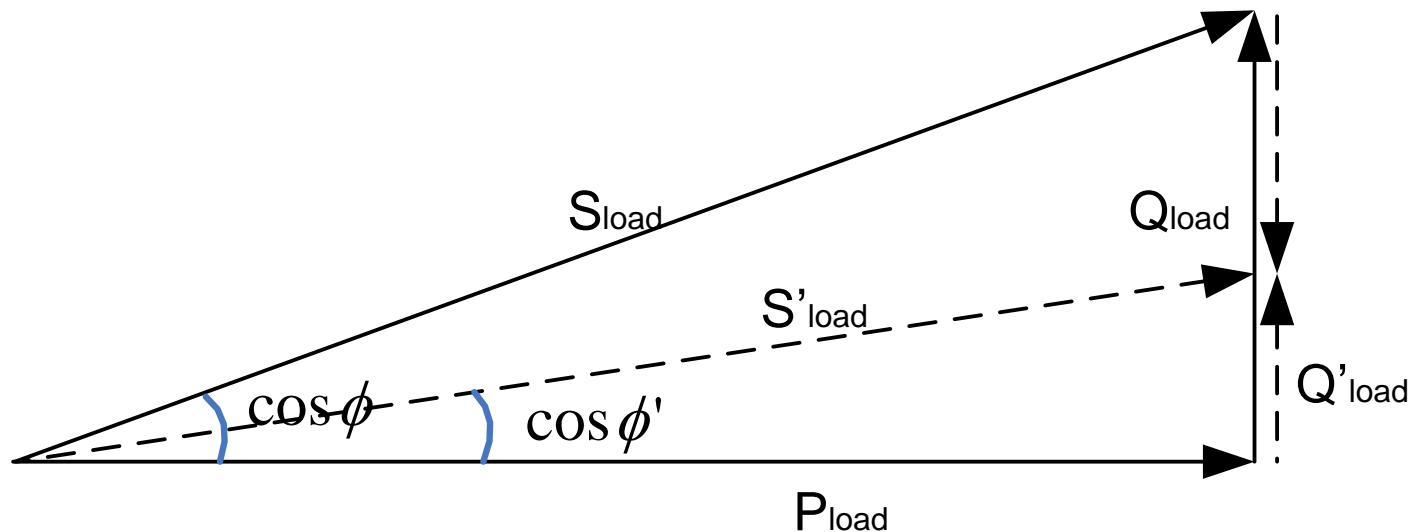
- When losses are not uniformly distributed over the circuit
  - Peak 3 $\phi$  Load Losses = “I-square R”  $\times$  Distribution Factor

$$\text{Distribution Factor} = 1 + I_r/I_s + (I_r/I_s)^2$$



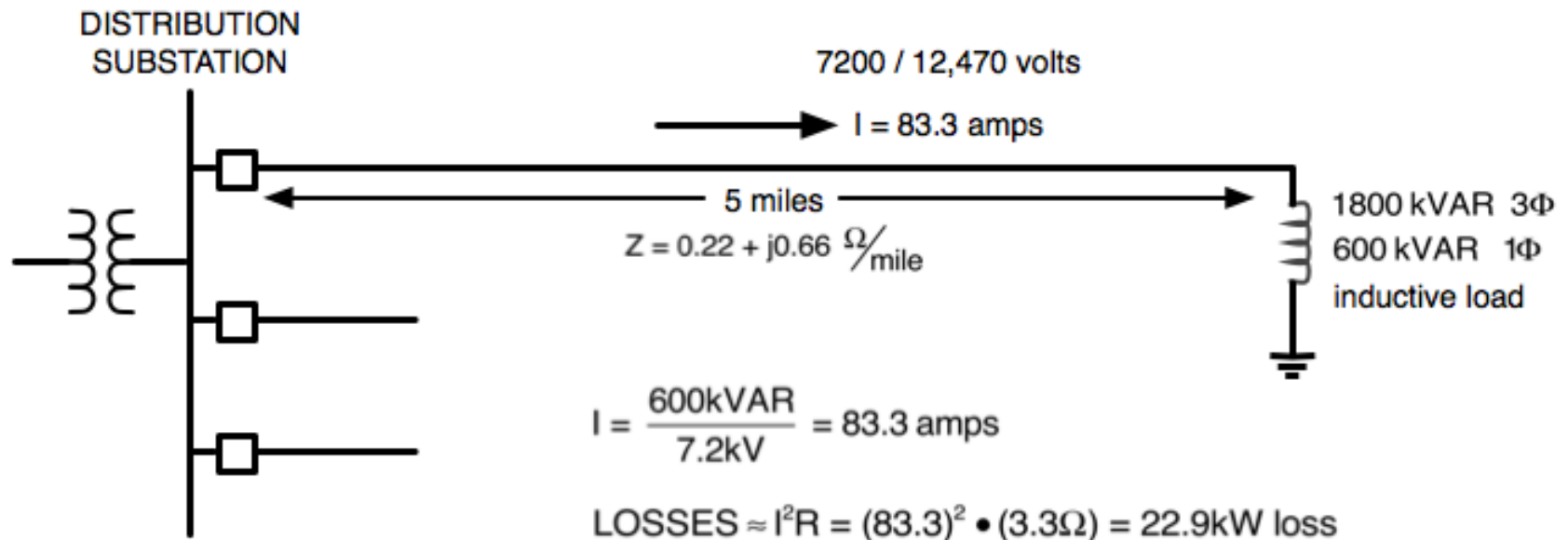
# Q/A

# Active and Reactive Power



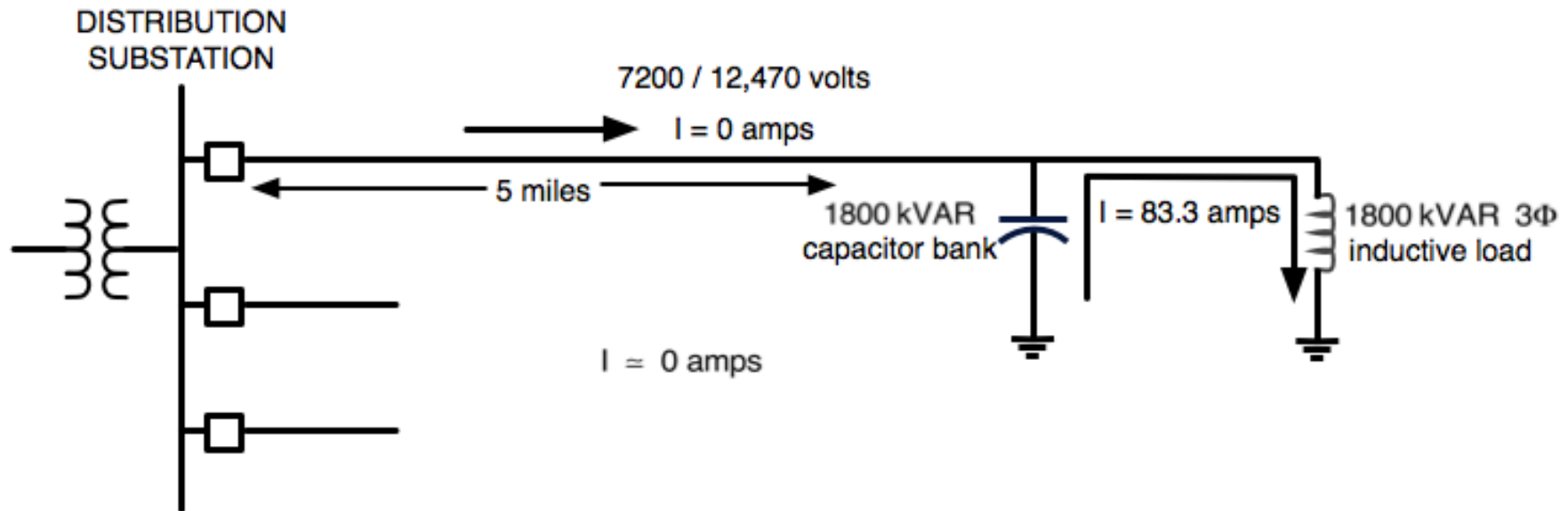
# Inductive Load

- 1800 kVAR inductive load



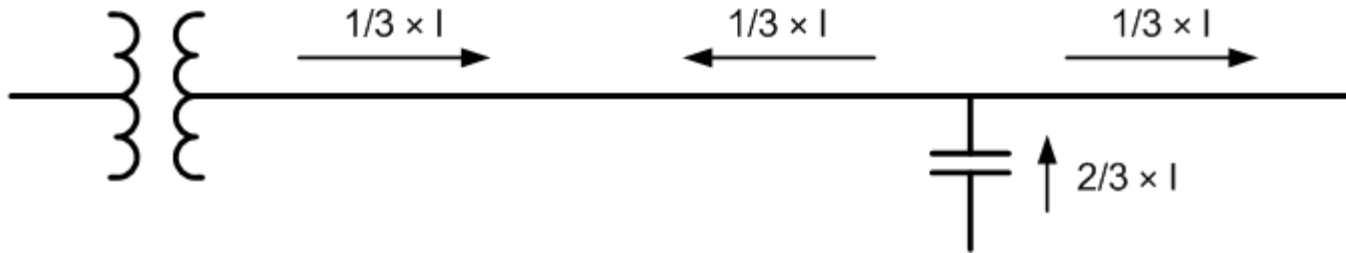
# Impact of Capacitor Bank

- 1800 kVAR capacitor bank



# Capacitor Placement

- 2/3 Rule



Place 2/3 of the needed kVAR 2/3 of the way down the feeder.

# Fixed/Switched Capacitors

- Loads change over time
  - 24 hours of the day
  - 7 days of a week
  - 12 months of a year
- Loads change due to weather
- Loads change due to human activities
- Challenges
  - Size, location, timing
  - Minimize costs and losses
  - Transmission constrains, etc.

# Capacitor Control

- Voltage
  - cheap & simple / ☹ for insignificant voltage drop
- Current
  - ☹ for high/low power factor (winter/summer) loads
- VAR
  - ☹ for multiple switched banks
- Temperature
  - cheap & simple / ☹ for special days
- Time
  - cheap & simple / ☹ for abnormal loads
- Power factor
- Automation
- Combination

# Capacitor Switching



# Q/A

# Thank You

- Questions / comments?

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